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A Scalable Wavelet Transform VLSI Architecturefor Real-Time Signal Processing in High-DensityIntra-Cortical Implants

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*Abstract—*This paper describes an area and power-efficient VLSI approach for implementing the discrete wavelet transform on streaming multielectrode neurophysiological data in real time. The VLSI implementation is based on the lifting scheme for wavelet computation using the symmlet4 basis with quantized coefficients and integer fixed-point data precision to minimize hardware demands. The proposed design is driven by the needto compress neural signals recorded with high-density microelec-trode arrays implanted in the cortex prior to data telemetry. Ourresults indicate that signal integrity is not compromised by quan-tization down to 5-bit filter coefficient and 10-bit data precision atintermediate stages. Furthermore, results from analog simulationand modeling show that a hardware-minimized computational core executing filter steps sequentially is advantageous over the pipeline approach commonly used in DWT implementations. The design is compared to that of a B-spline approach that minimizesthe number of multipliers at the expense of increasing the number of adders. The performance demonstrates that *in vivo* real-time DWT computation is feasible prior to data telemetry, permitting large savings in bandwidth requirements and communication costs given the severe limitations on size, energy consumption andpower dissipation of an implantable device.

*Index Terms—*B-spline, brain machine interface, lifting, micro-electrode arrays, neuralsignal processing, neuroprosthetic devices,wavelet transform.

INTRODUCTION

LSI implementation of the discrete wavelet transform(DWT) has
been widely explored in the literature as a result of the transform
efficiency and applicability to a widerance of signals particularly been widely explored in the literature as a result of the transform efficiency and applicability to a widerange of signals, particularly image and video [\[1\],](#page-14-0) [\[2\].](#page-14-0) These implementations are generally driven by the need to fulfill certain characteristics such as regularity, smoothness and linear

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phase of the scaling and wavelet filters, as well as perfect reconstruction of the decomposed signals [\[3\].](#page-14-0)

In some applications, it is desirable to meet certain design criteria for VLSI implementation to enhance the overall systemperformance. For example, minimizing area and energy con- sumption of the DWT chip is highly desirable in wireless sensor network applications where resources are very scarce. In addition to miniaturized size, minimizing power dissipation is strongly sought to minimize tissue

heating in some biomedical applications where the chip needs to be implanted subcuta- neously.

In this paper, we deal primarily with the design of DWT VLSI architecture for an intracortical implant application. Motivated by recent advances in microfabrication technology, hundreds of microelectrodes can be feasibly implanted in the vicinityof small populations of neurons in the cortex [\[4\], \[5\],](#page-14-0) opening new avenues for neuroscience research to unveil many mysteries about the connectivity and functionality of the nervous system at the single cell and population levels. Recent studies have shown that the activity of ensembles of cortical neurons monitored with these devices carry important information that can be used to extract control signals to drive neuroprosthetic limbs, thereby improving the lifestyle of severely

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paralyzed patients [\[6\]–\[8\].](#page-14-0)

One particular challenge with the implant technology is the need to transmit the *ultra-high* bandwidth neural data to the out- side world for further analysis. For example, a typical recording experiment with a 100 microelectrode array sampled at 25 kHzper channel with 12-bit precision yields an aggregate data rate of 30 Mbps which is well beyond the reach of state-of-the-art wireless telemetry. Other significant challenges consist of the need to fit circuitry within cm for the entire signal pro- cessing system, and operate the chip at very low power (no more than 8–10 mW) to prevent temperature rise above 1 C that may cause neural tissue damage. In previous studies, we have shownthat the DWT enables efficient compression of the neural data while maintaining high signal fidelity $[9]$ – $[11]$. To be imple-mented in an actual implanted device, chip size, computational complexity and signal fidelity must be balanced to create an op-timal applicationspecific integrated circuit (ASIC) design tai-lored to this application. Generally speaking, the case of computing the DWT for high throughput streaming data has not been fully explored $[12]$. It has been argued that a lifting scheme [\[13\]](#page-14-0) provides the fewest arithmetic operations and in-place computations, allowing larger savings in power consumption but at the expense of

Fig. 1. Block diagram of an implantable neural system illustrating the mixed signal processing proposed.

longer critical path than that of convolution-based ones [\[13\].R](#page-14-0)ecent work by Huang *et al.* [\[14\]](#page-14-0) focused on analyzing DWTarchitectures with respect to tradeoffs between critical pathand internal buffer implementations. Such critical path can beshortened using pipelining with additional registers or using a so-called *flipping* structure with fixed number of registers [\[15\].](#page-14-0) The *B-spline* approach [\[16\],](#page-14-0) on the other hand, requires fewer multipliers than lifting, replacing them with adders that maypermit a smaller chip area [\[17\].](#page-14-0) Nonetheless, most of the re- ported hardware approaches focus on computational speed and do not adequately address severe power and area constraints.By comparing with other implementations of the DWT in this paper, we demonstrate that the appropriate compromise among power, size and speed of computations is achieved with a sequential implementation of integer arithmetic lifting approach. The paper is organized as follows. In [Section I](#page-3-0)I, the classical single \mathcal{Q}_0 . channel one-dimensional (1-D) DWT and lifting DWT are introduced. [Section](#page-4-0) III describes the motivation for integer lifting DWT and approaches to efficiently map the algorithmto hardware for a single channel, single level DWT decomposi-tion. In Section IV, proposed architectures for integer lifting are described and analysed. π [Section](#page-9-0) V describes hardware consid- erations of $_n$ the proposed architecture for multiple channels and multiple L (levels of decomposition, and [Section](#page-13-0) VI describes performance comparisons and overall results.

THEORY

$$
\underline{a}^{j+1} = \underline{d}^{j+1}
$$

 $g_{\phi},g_{\gamma},\ldots,g_{\gamma}$

A typical state-of-the-art implantable neural interface systemas depicted in [Fig.](#page-3-0) 1 contains an analog front end consisting of pre-amplification, multiplexing and A/D
 $\frac{x_1x_2x_1}{x_1x_2}$: $g_1[i] - g_0[i] + C_1 \times f_0[i]$ conversion prior toextra-cutaneous transmission. An analog front end integrated onto a 64-electrode array would occupy 4.3 mm in 3 m tech-nology and would dissipate 0.8 mW of power [\[5\].](#page-14-0) This tradi- tional approach is not well suited for wireless data transmis- sion due to power demands associated with the resulting large data throughput. In the proposed approach, the power and chip area of the analog front end is reduced by using contemporary mixed-signal VLSI design approaches and more modern fabri- cation processes (e.g., 0.18 m), allowing advanced signal processing to take place within the implanted system without sig- nificant increase in the chip size. Power- and areaefficient im- plementations of the spatial filter, the DWT, and the encoder blocks would provide on-chip signal processing and data com- pression, enabling wireless transmission by reducing bandwidth requirements. In this paper, we only discuss VLSI implementa-tion of the DWT block. mostly contained in the short transients -or spikesabove the noise level that result from the activity of an unknown number of neurons. It can be observed that the sparsity introduced by the DWT compaction property enables very few "large" co- efficients to capture most of the spikes' energy, while leaving many "small" coefficients attributed to noise. This property per- mits the later ones to be thresholded [\[19\],](#page-14-0) yielding the denoisedsignal shown.

For near-optimal data compression, a wavelet basis needs to be selected to best approximate the neural signal waveform with the minimal number of data coefficients. A compromise be- tween signal fidelity and ease of hardware implementation has to be made. A near-optimal choice was proposed in [\[9\]](#page-14-0) from a compression standpoint and demonstrated that the *biorthog- onal* and the *symmlet*4 wavelet functions are advantageous overother wavelet basis families for processing neural signals. From a hardware implementation viewpoint, the *symmlet*4 family has much smaller support size for similar number of vanishing moments compared to the biorthogonal basis [\[20\]. I](#page-14-0)n addition, they can be implemented in operations.

A. Single Channel Lifting-Based Wavelet Transform

The lifting scheme [\[12\]](#page-14-0) illustrated in [Fig.](#page-3-1) 3 is an alternativeapproach to computing the DWT. It is based on three steps: First, splitting the data at level j into *even* and *odd* samples and , respectively; Second, predicting the odd samples from the evensamples such that the prediction error becomes the high passcoefficients ; and third, updating the even samples withto

obtain the approximation coefficients . This process is repeated times. At an arbitrary prediction and update step , the prediction and update filters $T_n(z)$ and

respectively, are obtained by factorizing the wavelet filters details and of the next level.

A lifting factorization of the *symmlet*4 wavelet basis amountsto the following filtering steps:

$$
s(q)2. \t f_1[i] - f_0[i] + C_2 \times g_1[i] + C_3 \times g_1[i+1]
$$

\n
$$
s(q)3: \t g_2[i] - g_1[i] + C_4 \times f_1[i] + C_5 \times f_1[i-1]
$$

\n
$$
s(q)4: \t a[i] - f_1[i] + C_5 \times g_2[i] + C_7 \times g_2[i-1]
$$

\n(7)

Alternatively, a B-spline approach for DWT computation [16] is based on factorizing the filters as

$$
H(z) \t\t h_a \t\t (8)
$$

where $Q(z)$ and $R(z)$ are known as the distributed parts, h_a and are normalization factors [\[17\],](#page-14-0) and are the orders of the*B-spline* parts, respectively. For the *symmlet*4, this factorizationcan be expressed as

 $H(z)$ (9)

where the coefficients B_1 through B_6 are listed in [Table](#page-3-1) II. Sincethe B-spline parts in both filters can be expressed as

$$
+ z^{-4} \tag{10}
$$

hey can be typically implemented using simple shifting and ad- dition. The polyphase decomposition similar to lifting can there- fore be performed on the distributed parts $R(z)$ and $Q(z)[16]$. This is achieved by splitting the distributed parts into odd and even components $R_e(z)$ and $R_o(z)$, $Q_e(z)$ and $Q_o(z)$, respec- tively. For example, the low-pass even distributed part can be represented as $R_e(z)$ B_2z^{-2} , and likewise for the re-maining components. The benefit in the B-spline method is a reduction in the number of floating point multiplications at theexpense of more additions [\[17\].](#page-14-0) [Table](#page-4-0) III compares the compu-tational requirements of lifting and B-spline DWT implemen- tations along with traditional convolution. In B-spline, four x4 multiplications are replaced by shifts and two x6 multiplications are replaced by shifts and additions . Relative to lifting, B-spline requires two fewer multiplications at the expense of ten more additions for one level of decomposition. Nevertheless, as the detailed lowpower/area DWT implementation below will show, any benefit to B-spline is diminished for multilevel multichannel decomposition.

B. Hardware Considerations

Power and area requirements of the DWT hardware are determined largely by the complexity of the computational circuitry and the required memory. To systematically reduce hardware requirements, we have explored different options to reduce computation and memory requirements at the algorithm level and analyzed their impact on signal integrity to determine an optimal approach. We summarize below two key ideasthat contribute largely to the reduction of circuit complexity and memory requirements that are discussed in subsequent sections, while more details of this analysis are further provided in [Section](#page-9-0) V.

1) Integer Approximation: Fixed-point integer approxima- tion limits the range and precision of data values but greatly re-duces the computational demand and memory requirements for processing and storage. To explore the potential of utilizing in-teger approximation in the proposed system, we observed that neural signal data will be entering the system through an A/D converter and will thus inherently be integer valued within a pre- scribed range. The data is first scaled to obtain data samples within a 10-bit integer precision. The integer approximation isthen computed for the scaled data. The integer-to-integer trans-formation [\[22\]](#page-14-0) involves rounding-off the result of the lifting fil-ters and $\ddot{\phi}$

$$
L(z)=(1+z^{-1})^{\gamma_2}R\mathbb{I}(z)\cdot l_a
$$

that are used to filter odd and even data samples, respectively. The last step that requires scaling by and G^{-1} is omitted. Hence, the dynamic range of the transform at each level will now change by \bigcap . As our results will demonstrate [\(Section V](#page-9-0)), the minimized circuit complexity

$$
L(z) = (1 + z^{-1})^4 (1 + B_{4z} - A_{3z} - A_{3z} - B_{4z} - A_{4z} - A_{4z}
$$

associated with integer representation should be well suited to this application provided that data precision is sufficient to maintain signal in- tegrity.

Quantization of the Filter Coefficients: Rounding-off wavelet filter coefficient values to yield a fixed point integer precision format can further reduce the computation and memory requirements. Implementing lifting-based wavelet transform with only integer computational hardware requires the filter coefficients be represented as integers along with the sampled data. [Tables](#page-3-1) I and [II](#page-3-1) show the scaled filter coefficients C_1 $C_8(\textbf{x}16)$ and B_1 $B_6(\textbf{x}2)$ for the *symmlet*4 basis. These coefficients are further quantized into integer values. The level of quantization has a significant impact on the complexity of computational hardware. We quantified the effect of the roundoff and quantization errors on the signal fidelity as a function ofmultiplier complexity [\[21\].](#page-14-0) Our results [\(Section](#page-9-0) V) demonstratethat 6 bits (5 bits 1 sign bit) coefficient quantization can adequately preserve signal integrity.

I. SINGLE-CHANNEL SINGLE-LEVEL HARDWARE DESIGN

In a first-order analysis, the area of a CMOS integrated circuit is proportional to the number of transistors required, and power consumption is proportional to the product of the number of transistors and the clocking frequency. Through transistor-level custom circuit design, circuit area and power consumption can be further reduced, with significant improvement in efficiency over field-programmable gate arrays (FPGA) or standard cell ASIC implementations.

Parallel execution of the DWT filter steps using a pipelined implementation is known to provide efficient hardware utiliza- tion and fast computation. In fact, a vast majority of the re- ported hardware implementations for lifting-based DWT rely on pipeline structures [\[20\], \[23\],](#page-14-0) [\[24\]. H](#page-14-1)owever, these circuits target image and video applications where speed has highest priority and the wavelet basis is chosen to optimize signal repre- sentation. A different approach is required to meet the power and area constraints imposed by implantability requirements, the low bandwidth of neural signals, and the type of signals ob- served. Two promising integer lifting DWT implementations, a pipeline approach and a sequential scheme, have been optimized and compared for the *symmlet4* factorization and data/coeffi- cient quantization described above. Furthermore, the hardware requirements for lifting DWT

have been compared to a B-spline implementation to verify the advantage of lifting in the applica-tion at hand.

A. Computation Core Design

z

To begin, notice that the arithmetic operations in the lifting scheme in [\(7\) h](#page-3-1)ave a noticeable regularity that permits any ar- bitrary step to be defined as

$$
= 1 \quad \text{such that} \quad O1^x = g^x + a^x \quad f^x
$$

$$
O_{ij}
$$

where $(1, , , ,$ and take the values of and f in [\(7\),](#page-3-1) and and b_i are the quantized filter coefficients given in [Table](#page-3-1) I. The regularity of this repeated operation indicates that an opti-mized integer DWT implementation would include a hardwareunit specifically designed to evaluate [\(11\).](#page-4-0) By tailoring this

cir-cuit to the near-optimal data and coefficient bit width describedabove, a single computation core (CC) suitable for all lifting

filter steps in [\(7\)](#page-3-1) can be obtained.

[Fig.](#page-5-0) 4 describes a CC block that was custom designed to min- imize transistor count and power consumption while supporting up to 10-bit data and 6-bit filter coefficients, both in signed integer formats. The CC employs a simple hardwired shifting operation to

1:
$$
O1^3 = h^3 + a
$$
 f^3

remove the x16 scaling factor from the quantized coefficients. It generates a 10-bit output and an overflow error bit, though the lifting scheme should inherently maintain results within 10-bit magnitude. Several multiplier topologies were ex-perimentally compared to define the most efficient option for

6 10-bit operations. A Wallace tree multiplier with modifiedBooth recoding was implemented along with a custom 3-term adder optimized for power rather than speed. The fixed x16 scaled integer coefficients were modified for Booth recording before being stored in onchip ROM to eliminate the need for

Fig. 4. Customized computation core for integer-lifting wavelet transform using binary scaled filter coefficients.

an on-chip encoder. The resulting circuit very efficiently imple-ments steps 2-4 of [\(7\)](#page-3-1) and can also compute steps 1 and 5 using a control signal that shuts off the unused multiplier to eliminateunnecessary power consumption.

B. Real-Time Integer DWT Processing Architectures

To identify the most efficient architecture for executing the entire set of lifting equations in real time on a continuous flowof input data samples, let us first re-define the filter equations in [\(7\) w](#page-3-1)ith a more hardware-friendly notation. Building on the concept of a fixed three-term computation core described above, the notation in [\(11\)](#page-4-0) can be used to rewrite [\(7\)](#page-3-1) at a specific cycle,

, as

$$
X \tV = 84r\beta^2 + \frac{Q_1^2 - f^4 + 4q}{Q_1^2 + 6q^2} + \frac{Q_2^2 - f^4 + 4q}{Q_1^2 + 6q^2} + \frac{Q_1^2 + 4q}{Q_1^2 + 6q^2} + \frac{Q_2^2}{Q_1^2 + 6q^2} + \frac{Q_2^2}{Q_1^2} + \frac{Q_2^2}{Q_1^
$$

where and f are the input data pair of samples, the outputs of steps 1–5 are $O1-O5$, coefficients C_1-C_8 have been replaced by \qquad - and b_2 b_4 to indicate the CC input to which they willbe applied, and the superscripts represent the computation cycle in which the data value was generated. The 2nd and 3rd terms in step 2 have been swapped to maintain a regular data flow described further below. Steps 2 and 5 require data from future computation cycles. Thus, in order to compute the five filter steps in real time, where all inputs must be available from prior computations, execution must span *three* computation cycles. During cycle the following five steps can be executed inreal time:

2:
$$
O2^2 - f^2 + a_2 O1^3 + b_2 O1^2
$$

\n3: $O3^2 - O1^2 + a_3 O2^2 + b_3 O2^4$
\n $\therefore O4^2 - O2^2 + a_4 O3^2 + b_4 O3^4$
\n $O5^1$ 04². (13)

 \times

 a_i

(11)

Notice that each step in [\(13\) r](#page-5-0)elies only on previously calculated data, provided these steps are performed *sequentially*. Having rearranged the terms in step 2 of [\(7\),](#page-3-1) the output of each step in

[\(13\) b](#page-5-0)ecomes the 2nd term input to the subsequent step, which is useful for efficient hardware implementation. Notice also that most of the data values needed are generated within the same

cycle; only the four values in [\(13\) w](#page-5-0)ith boldface type (two are re- peated twice) are generated in a previous cycle. Thus, if the filter steps are implemented sequentially, only *four* storage/delay reg- isters are required.

Although [\(13\)](#page-5-0) does allow real time computation of the filtersteps in sequence, dependencies within the steps

in [\(13\)](#page-5-0) pre-clude parallel execution necessary for a pipeline implementa-tion. To make each filter step

dependent only on data from priorcycles, execution must span *seven* data samples. During cyclethe following $r = 7$

sequence could be computed without any dependency on current or future cycle results:

$$
O1^{7} = h^{7} + a_{2} f^{7}
$$

$$
O2^{5} = f^{5} + a_{2} O1^{6} + b_{2} O1^{5}
$$

$$
O34 = O14 + a3 O24 + b3 O23
$$

\n
$$
O43 = O23 + a4 O33 + b4 O32
$$

\n
$$
O51 O42 (14)
$$

Here, the second term of each computation relies on the output from the preceding step during the previous computation cycle. In a pipeline, these four second-term data inputs could be held ina memory with one-cycle delay. The first and third terms require seven additional data values from prior cycles, one of which is needed twice, resulting in six independent values. One of the values (f^5) in step 2) needs a two-cycle delay, requiring an extra delay register. Thus, a total of 11 storage/delay registers wouldbe required to hold all of the necessary values from prior cyclesfor a pipeline implementation.

C. Pipeline Design

The integer DWT filter equations in [\(14\)](#page-5-0) can be implementedsimultaneously in a pipeline structure that permits real time,continuous signal processing to take place. Fig. [5\(a\)](#page-6-0) illustratesa pipeline structure designed around the customized three-termcomputation core from [Fig.](#page-5-0) 4. The output of each of the fivefilter stages is held by a darkly shaded pipeline register, andother registers provide the necessary delays. By clocking all of the registers out of phase from the CC blocks, continuous oper-ation is provided. The computation latency is seven cycles, dueto the five pipeline stages and the two delay cycles built int[o\(14\).](#page-5-0) The temporal latency for detail and approximationresults is 14 samples because each computation cycle op- erates on a pair of data samples. The overall pipelined *computa-tional node* consists of five CC blocks, 15 10-bit registers, andan 8 6b coefficient ROM. An additional delay phase could beadded at the $O4$ output to synchronize the latency of the detail

and approximation outputs.

D. Sequential Design

Although the pipeline structure achieves fast integer DWT processing via a large hardware overhead, it is very resource-ef- ficient and thus well suited for low-power, single channel, neural signal processing. However, as discussed below, scaling the pipeline for multiple data channels and/or multiple decomposi-tion levels begins to break down the efficiency of the pipeline structure. An alternative approach is to process each of the filter steps (or pipeline stages) sequentially using a single CC

 $-03 + a_5$

Fig. 5. (a) Pipeline structure for integer-lifting wavelet transform with data notations to match filter equations in [\(11\)](#page-4-0) at a single point in time. (b) Sequentialstructure over five operation phases for comparison to the pipeline structure.

(O4)

 \times

block and a fraction of the registers required by the pipeline. This approach takes advantage of the low bandwidth of neural signals that permits the CC to be clocked much faster than the input data sampling frequency (typically in the range of 25–40kHz).

Sequential processing of the integer DWT filter steps can be achieved using [\(13\),](#page-5-0) where each stage depends only on data from previous cycles or from same-cycle outputs generated in a preceding step. The simplicity of data dependencies relative to the pipeline structure can be observed from [Fig. 5\(b\), w](#page-6-0)hich illustrates the sequential structure in a format comparable to thepipeline. Here, each section of the circuit represents a temporalphase rather than a physical stage. An important observation is that significantly fewer registers are needed because the inputs of subsequent phases rely largely on preceding outputs from thesame computation cycle. Therefore, it can be shown that the overall sequential DWT circuit can be efficiently implemented with six 10-bit registers to manage data flow between computa-tion cycles, a single CC block, an 8 6b coefficient ROM, and a simple control block to direct data from memory to the appro- priate CC input during each phase of operation. Sequential exe-cution has a computation latency of *two* cycles, and the temporal latency for detail and approximation results is *four* samples.

E. Analysis and Comparison

As stated above, the sequential approach requires only one CC unit and six 10-bit memory registers compared to five CC units and 15 registers for the pipeline circuit. The sequential de- sign does, however, require additional multiplexers and controllogic to redirect data and coefficients to CC inputs, which are not necessary in the inherently hardware-efficient pipeline design.This added circuitry will make the critical path of the sequentialcircuit longer than that of the pipeline structure. Furthermore, to maintain the same throughput, the sequential design must be operated at five times the clock rate of the pipeline. Because data is processed in a real-time streaming mode, neither approach requires a large input data buffer.

Both architectures have been thoroughly analyzed to deter- mine which approach is best suited to the power and area re- quirements of an implantable neural signal processor. To first validate that both approaches can achieve the application speed requirements, a custom computation core has been implemented in CMOS, and analog simulations show the critical path delay is 6.5 ns in 0.5- m technology. Thus, approximately 6000 compu- tation cycles could be preformed within a

custom ralcircuit layouts shows that a single value for reason-ably approximates all of the integer

DWT blocks, especially forcomparing two similar circuits. Conservative values of 80 m per transistor for 0.5- m technology and 5 m per transistorfor 0.13- m technology have been selected to estimate the re-quired chip real estate.

TABLE IV CHARACTERISTICS OF SINGLE-LEVEL, SINGLE-CHANNEL INTEGER DWTHARDWARE FOR PIPELINE AND SEQUENTIAL CONFIGURATIONS AT TWO TECHNOLOGY NODES

		0.5um CMOS		0.13um CMOS	
×	transistors	area fmm^2	power [uW]	area \lceil mm ² \rceil	power [µW]
Pipeline	23,336	1.867	15.10	0.117	0.71
Sequential	7.931	0.634	18.55	0.040	0.87

Although absolute power consumption is inherently difficult to estimate, for the purpose of comparing the two design alter-natives, dynamic power can be determined as

$$
P = k \quad VDD^2 \quad f_s \quad \sum_i N_i \quad s_i
$$
\n
$$
(16)
$$

where *VDD* is the supply voltage and $\int_{\mathbb{R}}$ is the data sampling fre- quency (nominally 25 kHz). The parameter $\frac{1}{2}$ accounts for the average output load capacitance, the average number of tran- sistors per output transition, and the average output transitionsper clock cycle. This parameter is a function of both fabrication process and circuit topology and has been derived empirically as 3 and 0.75 fF for 0.5 m and 0.13- m technology, respec- tively. The variable is the clock rate scaling factor relative to f_s for each block such that the clocking frequency of each cir- cuit block is f_s . For example, in the pipeline configuration, the computation core will be clocked only every other cycle, i.e., $1/2f_{\rm s}$, so that the first of the pair of samples to be processed can be acquired in the idle cycle. Correspondingly, because the se-quential configuration must be clocked at five times the rate of the pipeline, it will have an average clocking rate of . In the pipeline approach, all of the blocks are nominal 25-kHz sam-pling frequency for neural signals. This indicates that speed is not a critical design constraint and that circuit optimization canfocus on chip area and power consumption.

Using custom design techniques, the chip area, A , required to implement both approaches will be roughly proportional to thenumber of transistors in the circuit

$$
-\sum_{i} T_{i} N_{i} \tag{15}
$$

where is the area per transistor λ and is the number of tran-sistorsin the th circuit block. Empirical observations of seve Τ

> clocked at the same frequency, except the coefficient memory that is static in both designs. In the sequential

implementation, one of the multipliersis idle during two of μ the five stages, so we estimate the sequen- tial CC clock scaling factor to be 2. Similarly, in the sequentialcontroller, most of the circuits are clocked at while othersare clocked at , so we estimate its clock scaling factor tobe 2 as well.

[Table IV l](#page-7-0)ists the total number of transistors in each approach along with the area and power estimated from [\(15\)](#page-6-0) and [\(16\)](#page-7-0) for both 0.5 m and 0.13- m technology. As expected, the pipelinecomputation unit requires nearly three times the area of the se- quential approach and would occupy about 21% of the chip area on a 3 3 mm chip in 0.5 m technology or 5% of a

1.5 1.5 mm chip in a 0.13- m process. The power model pre- dicts that the sequential approach will consume only 23% more power than the pipeline. The larger power consumption of the sequential approach can be attributed to its requirement for a more complex controller and the need to move more data around within the single computation core. Overall, these results show a tradeoff between area and power consumption between the twoapproaches.

F. Lifting Versus B-Spline

As an alternative to lifting, the B-spline method was investi-gated because it permits a reduction in the number of floating

point multiplications at the expense of more additions. How- ever, as demonstrated above, for implantable applications, in- teger processing is preferred. [Table III](#page-4-0) shows that B-spline saves two multiplications at the cost of 10 additions per cycle com- pared to lifting. Designs using Verilog synthesized to a customlibrary have shown that, for a pipeline implementation, B-spline requires significantly less 24-bit floating point hardware, but for integer processing (with 10-bit data and 6-bit coefficients) B-spline saves only 6% compared to lifting [\[25\]. F](#page-14-1)urthermore, B-spline can not be as efficiently implemented in a sequential structure, where lifting has been shown to require only 53% of the B-spline hardware resources for integer DWT. While B-spline implementations do have slightly less delay, speed is not a design constraint. Relative memory requirements are a more important issue in multichannel implementations as we show next.

II. MULTILEVEL AND MULTICHANNEL INTEGER DWTIMPLEMENTATION

A. Hardware Design

In implantable neuroprosthetic applications where a typical microelectrode array has many electrodes integrated on a single device, there is a strong need to support integer DWT computa-tions with multiple levels of decomposition for multiple signal channels pseudosimultaneously (i.e., within one sampling pe- riod). The lifting scheme and the two integer DWT implementa- tions described above have been chosen because of their ability to scale to an arbitrary number of channels and levels. Consid- ering that both of the single channel, single level, integer DWT approaches discussed above require a substantial portion of a small chip, it is unreasonable to pursue a hardware intensive solution that utilizes a "copy" of the circuit for each channel and level. This would dramatically increase circuit area beyond limitations for implantable systems. Given the available com- putation bandwidth of the CC block, the more appropriate solu- tion is to scale the clocking frequency as needed to sequentially compute filter equations for multiple channels and/or levels. Although clock scaling will still cause power to increase with channel and level, the circuit area required will be minimized and the power density can be held within the acceptable appli-cation limits.

Both the pipeline and sequential architectures can be scaled to multiple channels and/or levels by reusing the computationalnode hardware and increasing the clocking frequency to com- plete all computations within the input sample period. In both approaches, registers within the computational node hold data necessary for the next cycle's calculation. To sequentially reuse the computational node, some register values for a specific

channel/level must be saved so they will be available when that channel/level is next processed in a future cycle. [Fig. 6 s](#page-8-0)hows the multichannel, multilevel, implementations of the pipeline and sequential configurations.

1) Multichannel Considerations: In scaling the system to multiple data channels, the computation clock rate is scaled by the number of channels and a new memory block is added to save critical register data for each channel. For the pipeline, the 11 registers must be stored, while for the sequential circuit only

Fig. 6. Multilevel, multichannel implementations of (a) pipeline structure and (b) sequential structure.

four registers need to be saved. These registers are marked withan "s" in [Fig. 4](#page-5-0). An on-chip SRAM can be interfaced to the computational node to store register values, and the size of theSRAM will grow linearly with the number of channels. Note for comparison that a sequential B-spline implementation requireseight register values to be stored.

2) Multilevel Considerations: When expanding the DWT to multiple levels, notice that each level of dyadic DWT decom- position introduces only half the number of computations as the previous level. More explicitly, the number of results, μ per number of samples, , for an arbitrary level j can be expressedas

$$
\frac{R}{n} = \sum_{i=1}^{n} \left(\frac{1}{2}\right)^{i} \tag{17}
$$

 -0.5

Nc

which is always less than twice the number of samples. Con-sider also that, to process multichannel input pairs, before eachcomputation cycle the system must implement one idle cycle,wherein the first input of the pair is stored for each channel.Thus, if the level-one computations are executed in, say, the evencycles, the higher level computations can be executed in the oddcycles [\[26\]](#page-14-1) while input samples (one of the pair) are being storedfor the next level-one computation. This is illustrated in [Fig.](#page-8-0) 7.If we define the

B. Area and Power Modeling

For multiple channels/levels, the need to copy the entire set of pipeline registers to memory effectively negates one of the pri-mary advantages of the pipeline over the sequential approach. On the other hand, the sequential processing circuit is inherently designed to swap new data in/out each clock cycle. To quantita- tively compare these two approaches, circuit models have been developed to describe the power and area for each option as a function of the number of channels and the number of decom- position levels. The following models assume the hardware (in-cluding control logic) has been scaled to manage multiple chan- nels and levels, though they are still valid for single channel, single level implementations.

> analysis since both approaches consist of similar arithmetic and memory blocks.

> Using [\(16\),](#page-7-0) a general expression for power consumption as a function of channels and levels, which is valid for both approaches being considered, is given by

$$
P = 2 \cdot k \quad VDD^{2} \quad fs \quad \sum_{i} \left(N\omega_{i} + (C - 1) \quad L \quad N\omega_{i} \right)
$$

$$
+ (L - 1) \quad C \quad N\psi(Cf_{i} \quad L\omega_{i} \quad s_{i}) \quad (20)
$$

where $\int f_i$ is the channel clock frequency scaling factors, $L u_i$ is a level usage factor, and all other variables are as previously

usage rate, , as the average number of cycles for a single computation to occur, then for the first decomposition level the usage rate is one half, i.e., $U(1)$, and the computational hardware is idle during the other half ofthe cycles. Moreover, approaches 1.0 as the number of

levels increase, i.e.,

 $U(L) = 1 - 2^{-L}$ Fig. 7. Sequential processing scheme for multilevel, multichannel computa- tion. At the top of this sequence, one DWT result is available at each decompo-sition level. With the four levels shown, one idle computation cycle will occur every 16 cycles.

As the number of levels increases, the usage rate will increase toward maximum utilization without increasing computation frequency. For each level of decomposition beyond the first, one memory block per channel is required to store values held in the computational node registers. The registers to be stored are the same as those described in the multichannel case above.

A general expression for calculating the area of both the pipeline and the sequential approaches as a function of channelsand levels is:

$$
A = A_t \sum_{i} (N\alpha_i + (C - 1) - L \cdot N\alpha_i + (L - 1) - C \cdot N\lambda_i)
$$
\n(19)

where A_t is the technology-dependent, empiricallyderived av-erage area per transistor, $N\mathfrak{o}_i$ is the number of transistors thatremain constant with level and channel in the th circuit block, and Nl are the number of

transistors that scale with channel and level, respectively, \int is the number of channels, and is is is the routing area, it is very useful for comparative routing area, it is very useful for comparative routing area, it is very useful for comparative routing area,

defined. Recall that the clock scaling factor was chosen to accommodate the fact that, in single level designs, every other cycle was idle while the data pair was being collected. To maintain a consistent definition of variables in multilevelimplementations, which utilize the idle cyclesto process all higher levels, the factor of 2 is introduced at the beginning of [\(20\).](#page-9-0)

Both the pipeline and sequential architectures have been developed to define the model parameters given in [Table V, w](#page-10-0)hich are valid for $\overline{I} > 1$ and $\overline{C} > 1$. The computational node circuitry, including control logic, has been scaled up to manage an arbitrary number of levels and channels, with negligible per channel/level increase in complexity. Thus, only data memory increases with the number of channels. Clocking frequency of the computational node circuits must scale with channel, while each memory block is only accessed once per cycle regardless of the number of channels. The controller frequency scales linearly with channel but is assumed to remain constant with level. For all other circuit blocks, the usage rate $U(L)$ accounts for inactive computation cycles.

V. RESULTS AND DISCUSSION

A. Signal Integrity

We have assessed the effects of data and filter coefficient ap-proximations on the quality of the signals obtained after recon-struction. We quantified the performance in terms of the com-plexity of hardware required to implement [\(7\)](#page-3-1) and illustrated theresults i[n Fig. 8](#page-9-0). The wavelet filter coefficients were quantizedto different resolutions ranging from 4 to 12 bits, with the 6-bitvalues given in [Table](#page-3-1) I. The data was also quantized in the samerange. The *effective* signal-to-noise ratio (eSNR), defined as the log ratio in dB of the peak spike power to the background noisepower is illustrated in Fig. [8\(a\)](#page-9-0) versus multiplier complexity in equivalent bit addition/sample for an average input SNR of 6dB. These results demonstrate that, with sufficient precision, theuse of integer computations does not result in significant signaldegradation as quantified by the observed output SNR. Specifi-cally, with quantization of filter

the frequency range of neural spike trains and local field

TABLE V

MODEL PARAMETERS FOR AREA AND POWER CALCULATIONS

* accounts for average usage at 2.5 clock scale

coefficients to 6 bits and data to10 bits, the output SNR is within 1% of its average input value.In Fig. [8\(b\),](#page-9-0) the spectrum of the residual quantization and round-off noise is also illustrated to demonstrate the loss in thesignal power-spectral density in different cases. In the case of4 bit quantization of the filter coefficients, the residual noisefrequency content is closest to that of the original signal in thelow frequency range (subband 0–1 kHz), indicating that somesignal loss may have occurred in that band. On the other hand, Fig. 8. (a) Effect of round off and quantization errors on the signal fidelity as a function of multiplier complexity. (b) Power-spectral density of the original data and the residual noise for integer approximated data and quantized waveletfilter coefficients for various bit widths. (c) Example spike waveforms obtainedin each case.

filter quantization of 6 bit or higher results in residual noise thatconsists of high frequency components above 8 kHz, which is outside

Fig. 9. Comparison of multichannel/multilevel pipeline and sequential integerDWT approaches: relative chip area and relative power consumption versus number of levels and channels.

potentials (LFPs) [\[27\].](#page-14-1) A representative example of spike wave- forms in each case is illustrated in [Fig. 8\(c\) t](#page-9-0)o demonstrate thevery negligible effect of this process on the quality of the av- erage spike waveform. Taking these results all together, it is clear that the choice of 6/10-bit coefficient/data quantization offers the best compromise among multiplier complexity and signal fidelity as concluded earlier.

We should emphasize that perfect reconstruction of signals off chip may not be always needed. Typically, neural signals contain the activity of multiple neurons that need to be *sorted out*, and this information remains in the compressed data at the output of the DWT block. We have shown elsewhere that sorting the multi source neuronal signals can be performed directly onthe wavelet transformed data [\[10\],](#page-14-0) [\[28\],](#page-14-0) and this topic is outside the scope of this paper.

B. Multichannel/Level Implementations

Using [\(19\)](#page-8-0) and [Table](#page-10-0) V, the relative area for pipeline and sequential architectures as a function of levels and channels is shown in [Fig.](#page-10-0) 9. These results demonstrate that the pipeline re- quires significantly more chip area than the sequential approach and its area needs grow faster with larger number of channels and levels. This is due primarily to the relatively large number of registers that must be stored per channel or level (11 for pipeline compared to 4 for sequential). [Fig.](#page-10-0) 9 also shows the relative

Fig. 10. Power-area product versus level and channel for pipeline and sequen-tial approaches.

power consumption for the two approaches based on [\(20\). T](#page-9-0)helinear increase in power per channel is slightly higher with the sequential design than the pipeline. Although there is a sharp jump in power from to

, further increases in levels require less and less additional power as the usage rate approaches one. The most important observation from [Fig.](#page-10-0) 9 is that the power consumption of the two implementations is al- most similar but the sequential design requires significantly less chip area.

Due to size and power constraints in implantable systems, an important figure of merit is the relative areapower product,which is plotted i[n Fig. 10 v](#page-10-0)ersus both level and channel. [Fig. 10](#page-10-0) illustrates that the sequential approach is increasingly prefer- able as the number of channels or the number of decomposi- tion levels increases. The only significant benefits of the pipeline within the enforced design constraints are that it can be clockedat a higher rate and that it takes fewer clock cycles

to complete a computation. Both of these factors result in the pipeline having a *higher threshold* on the maximum number of channels that can be simultaneously processed. However, based on the parameters defined above, the sequential execution architecture has an esti- mated maximum of around 500 data channels (at). Given the chip area limitations, the area-efficient sequential approachis best suited for this application. In an example implementa- tion with 32 channels and 4 levels of decomposition, the models predict that the sequential approach will require 0.692 mm and

50.1 in 0.13- m CMOS, indicating the feasibility of performing front-end signal processing within the constraints of animplanted device.

Another interesting result of this study is the comparison of the area required by the computational node circuitry versus the area required by the memory that holds register values required for multichannel/multilevel operation. [Fig.](#page-13-0) 11 illustrates this re-sult for both sequential and pipeline configurations as a func- tion of channels at . Notice with the pipeline that memory dominates the area when the number of channels is greater than four. For the sequential design, memory dominates when the number of channels is greater than ten. With 10-bit data resolution, at and $\left(\frac{1}{2}\right)$, the pipeline requires over 14 000 bits

 μ W μ

$$
L = 4
$$

 $L = 4$ -32

Fig. 11. Relative area versus channels of data memory compared to all other blocks for sequential and pipeline designs, at $L = 4$.

of SRAM, while the sequential circuit requires only about 5000 bits. Reducing memory requirements becomes increasingly im-portant in multichannel applications, again highlighting the ad-vantage of the sequential approach.

C. Lifting versus B-Spline

As illustrated in [Fig.](#page-13-0) 11, the memory required to store intermediate calculation values will dominate circuit area in multichannel implementations. Careful analysis of an opti- mized sequential B-spline implementation [\[25\]](#page-14-1) has shown that eight memory registers are required per channel/level, compared to four for sequential lifting and 11 for pipeline lifting. Based on this information and the comparisons above, B-spline has a slight advantage over pipeline lifting but incurs a significant penalty relative to sequential lifting in terms of area. Furthermore, the sequential lifting implementation requires only about 25% of the dynamic power of sequential B-spline, primarily because B-spline takes 18 cycles to exe- cute sequentially compared to 5 cycles for lifting [\[25\].](#page-14-1) The advantage of sequential lifting becomes even more profound when static power is considered, especially in deep submicron technologies. [Fig.](#page-14-0) 12 provides an additional comparison, wherethe number of required gates, synthesized from Verilog descrip- tions of lifting and B-spline circuits, are plotted. These results illustrate that lifting is increasingly preferable over B-spline as the number of channels and levels increase.

D. Multiplication-Free Lifting

The CC unit proposed in this paper uses one multiplier so that the calculations required per sample are 8 multiplications and 8 additions that can be completed in 5 cycles as listed in [Table](#page-4-0) III.It is noteworthy that a general purpose lifting approach based on only shifts and additions

was proposed in [\[3\]. F](#page-14-0)or the sake of completeness, we compared the demands of a CC unit with a multiplier (proposed in this paper) to a CC unit without a mul-tiplier, i.e., composed of only a shifter and an adder. The later

approach resulted in 12 shift operations and 21 add operations, and required 21 cycles per sample. This is because the equa- tions required to compute multiplication-free lifting DWT did not show any regular structure such as the ones in [\(7\). T](#page-3-1)here- fore, substituting another adder and shifter in the data path did not help in reducing the number of cycles required to completethe computation. With respect to area demands, we found that for one sample pair, a CC unit without a multiplier requires 52% less area compared to a CC with multiplier. This obvi- ously translates into large savings in chip area. However, thesesavings were not substantial when the system is scaled up. For example, a 32 channel/4-level DWT system using a CC with multiplier would occupy 6.5% of the total chip area as opposedto 3.3% using a CC without multiplier. So the overall savings in chip area are only 3.2%. In contrast, the CC without multiplierrequires 13.3% more power than a CC with multiplier for this specification. We therefore concluded that the reduction in area using a shift and add strategy in the lifting approach is overshad- owed by the increase in power dissipation when multichannel/ multilevel decomposition is sought.

CONCLUSION

VLSI architectures to compute a 1-D DWT for realtime multichannel streaming data under stringent area and power constraints have been developed. The implementations are based on the lifting-scheme for wavelet computation and integer fixed-point precision arithmetic, which minimize com- putational load and memory requirements. A computational node has been custom designed for the quantized integer lifting DWT and characterized to estimate the maximum achievable computation frequency. Negligible degradation in the signal fidelity as a result of these approximations has been demon- strated.

Detailed comparison between the lifting and the Bspline schemes was presented. It was shown that the lifting approach is more suited when floating point operations are eliminated, thereby superseding the gain achieved by the B-spline ap- proach where adders replace multipliers. Two power and size efficient hardware alternatives for computing the single-level, single-channel wavelet transform have been described andanalyzed. The memory management efficiency of the pipeline design results in slightly less power dissipation, while the se- quential execution design requires significantly less chip area. Design considerations for scaling these architectures to multi- channel and multilevel processing have been discussed. Area and power consumption models with detailed transistor count and switching frequency parameters have been described and used to compare the performance of the

two design alternatives in multichannel and multilevel implementations. The results show many interesting characteristics of each design when it scales to an arbitrary number of levels and channels. When the number of channels is two or more, the sequential execution architecture was shown to be more efficient than the pipeline approach in terms of both power and chip area. Furthermore, results indicate that, using this architecture, multilevel pro- cessing of many channels simultaneously is

> feasible within the constraints of a high-density intracortical im- plant. This work demonstrates that on-chip real-time wavelet computation is feasible prior to data transmission, permitting large savings in bandwidth requirements and communication costs. This can substantially improve the overall performance of next generation implantable neuroprosthetic devices and brain-machine interfaces.

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Fig. 12. Total number of gates as a function of the number of channels and the number of levels for the lifting and B-spline implementation.

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